



Arden Primary School Calculation Policy

Maths Mastery at Arden

At Arden, we recognise that Maths is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. In providing a high-quality maths education, we allow our children to understand the world, reason mathematically, appreciate the beauty and power of mathematics and develop a sense of curiosity and enjoyment for the subject.

Mastering maths means pupils acquire a deep, long-term, secure and adaptable understanding of the subject that is solid enough to enable them to move on to more advanced material in the future. True mastery aims to develop all children's mathematical understanding at the same pace. As much as possible, children should be accessing the same learning. Differentiation should primarily be through support, scaffolding and deepening, not through task. At Arden, we teach in mixed ability classes with mixed ability talk partners. Aspire challenges are used to deepen understanding.

Stem Sentences

Stem sentences encourage and structure a child's thinking and their ability to articulate this. At Arden, we have some generic sentence stems that are used in all year group settings in order to support the explanations given by children. From Nursery to Year 6, our children are encouraged to explain, justify, argue, describe relationships, prove and enquire.

Vocabulary

The use of accurate mathematical vocabulary that is consistently understood across the primary setting is key to ensuring a solid understanding of the mathematical concepts. Children at Arden are encouraged to use accurate vocabulary from Nursery to Year 6 which is modelled by all staff.

Concrete, pictorial and abstract approach

We believe that children gain a more secure grasp of mathematical concepts through contextual exploration using concrete resources such as cubes, base ten and counters. The use of concrete resources is then supported through appropriate pictorial representations such as bar models and part, part, whole models. Once the conceptual understanding has been achieved through concrete and pictorial means, children will then move on to exploring abstract representations.

Fluency, reasoning and problem solving

We place a high emphasis on the learning of times tables facts and other number facts through varied and frequent practice, in order that children can recall and apply knowledge rapidly and accurately. Children are encouraged to reason using appropriate mathematical vocabulary and apply their mathematical knowledge to solving problems.

Some content taken/adapted from:



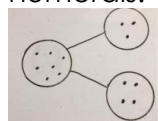
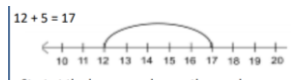
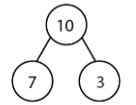
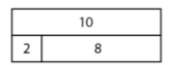
DfE National Curriculum

NCETM

White Rose Maths



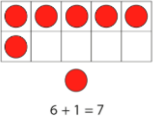
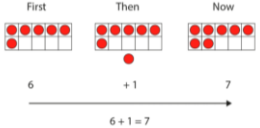
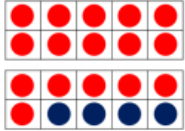


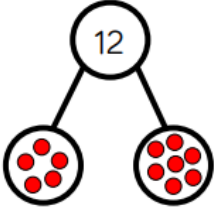
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Addition					
Objective and strategy	Concrete	Pictorial	Abstract	Sentence Stems for all year groups	Vocabulary for all year groups
<p>EYFS and Year 1</p> <p>Combining two parts to make a whole: part whole model.</p> <p>Starting at the bigger number and counting on- using cubes.</p>	<p>Use cubes and other objects to add numbers together as a group or in a bar.</p>  <p>Start at the bigger number and count on. Represent the number lines using bead strings or cubes.</p> 	<p>Represent the cubes using dots or crosses. Use a part whole model with dots progressing to numerals.</p>  <p>Start at the larger number on the number line and count on in ones or one big jump to find the total.</p>  <p>Draw the ten frame</p>	 <p>3 is a part, 7 is a part and the whole is 10. $7 + 3 = 10$ $10 = 7 + 3$</p>  <p>Place the larger number in your head and count on the smaller number to find your answer.</p> <p>Explore equality in different ways.</p> $6 + _ = 11$ $6 + 5 = 5 + _$ $6 + 5 = _ + 4$	<p>_____ is more than/bigger than/taller than/heavier than _____</p> <p>_____ is the same as _____</p> <p>There are more _____ than _____</p> <p>I know _____ because _____</p> <p>There are _____ and _____. We can write this as _____ plus _____.</p> <p>_____ is equal to _____ plus _____.</p> <p>_____ and _____ are the addends.</p>	<p>subitising - instantly recognising an amount.</p> <p>unitising -treating groups that contain or represent the same number of things as ones.</p> <p>sum</p> <p>total</p> <p>parts and wholes</p> <p>plus</p> <p>altogether</p> <p>add</p> <p>more</p> <p>is equal to</p>

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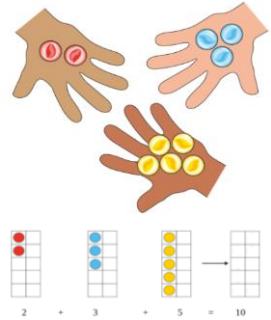
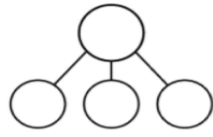
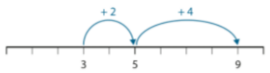
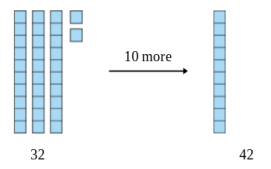
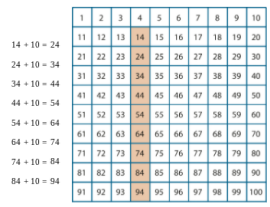
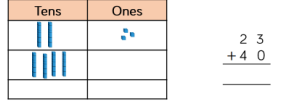


Arden Primary School Calculation Policy

<p>Regrouping to make 10 using ten frame.</p> <p>Represent and use number bonds and related subtraction facts within 20.</p>	<p>Start with the bigger number then use the smaller number to make ten using a ten frame.</p>  <p>$6 + 1 = 7$</p>  <p>First Then Now</p> <p>$6 + 1 = 7$</p> <p>Represent number bonds using ten frames and bead strings.</p> 	<p>and counters/cubes.</p>   <p>First Then Now</p> <p>$1 + 3 = 4$</p> <p>Show number bonds using the part, part, whole model and counters.</p> 	<p>Record number bonds systematically and look for patterns:</p> <p>$12 = 0 + 12$ $12 = 1 + 11$ $12 = 2 + 10...$</p>	<p>I know that ____ plus ____ is equal to ____ so ____ plus ____ is equal to ____.</p> <p>There are ____, ____ and ____, altogether there are ____.</p> <p>If ____ plus ____ equals ____ then ____ plus ____ equals ____.</p> <p>First...then...now...</p> <p>The sum has increased by ____; one addend has stayed the same, so the other addend must increase by ____.</p>	<p>is the same as</p> <p>addends</p> <p>addend + addend = sum</p> <p>exchanging</p> <p>commutative law - a sum or product can be calculated in any order (e.g. $ab = ba$).</p> <p>associative law - we can group numbers in any order when adding or multiplying (e.g. $(a + b) + c = (b + c) + a$)</p>
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<p>Year 2</p> <p>Adding three single digits.</p>	<p>Use counters and cubes to combine three amounts. Show using the ten frame.</p> 	<p>Represent using counters on a part, part, part, whole model.</p>  <p>$10 = 2 + 3 + 5$</p>	<p>Show using a number line before representing as a number sentence. Bridge to ten first as appropriate.</p> 	<p>Do I need to make an exchange?</p> <p>What has stayed the same?</p> <p>What has changed?</p>	<p>distributive law - $a \times (b + c) = (a \times b) + (a \times c)$</p> <p>inverse</p>
<p>Adding multiples of ten.</p>	<p>Model using base ten.</p> 	<p>Recognise patterns in a 100 square and on the Gattegno Chart.</p> 	<p>Represent the calculation on a number line and using the column method (with base ten) where appropriate.</p> 		

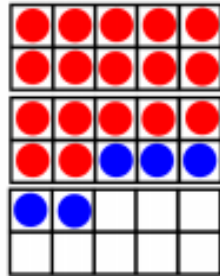
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Add TO + O.

Use ten frame to bridge to ten.

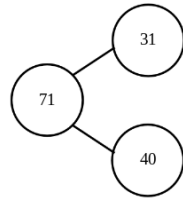


$$17 + 5 = 22$$

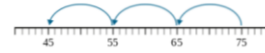
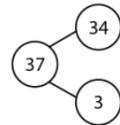
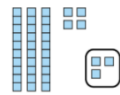
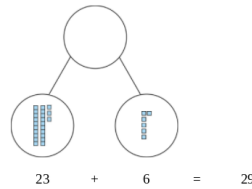
Use base ten to represent the calculation.

1000	2000	3000	4000	5000	6000	7000	8000	9000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

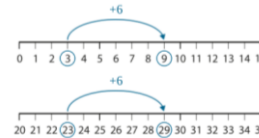
Represent using a part, part, whole model.



Represent as a part, part, whole model.



Show on a number line and use the column method in its expanded or shortened form as appropriate. Make connections with related facts.





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Add TO + TO.

Tens	Ones	2 8
		+ 7
		3 5
		1

Use base ten to partition two 2-digit numbers and regroup to make ten.

£40 £5 £20 £3 = £68

$40 + 5 + 20 + 3 = 68$

$40 + 5 = 45$

$20 + 3 = 23$

$45 + 23 = 68$

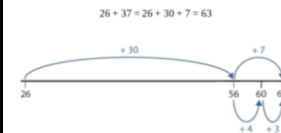
Find the sum of 34 and 23

	Tens	Ones
34		
+ 23		
+		
=		

Use bar models to support. Represent the base ten using symbols.

Tens	Ones	2 8	2 8
		+ 7	+
		3 5	7
		1	1 5
			2 0
			3 5

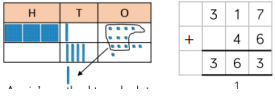
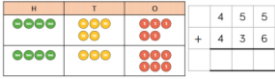
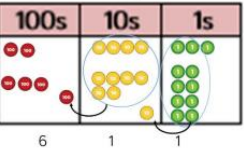
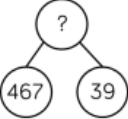
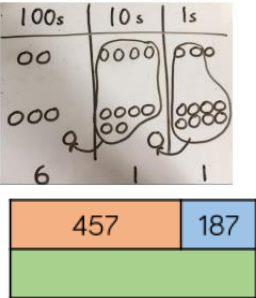
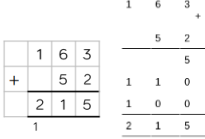
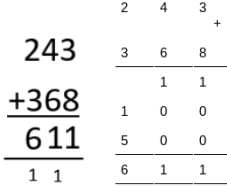
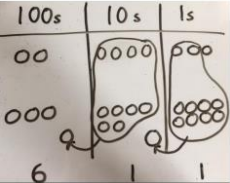

Show calculations on a number line, bridging the ten where necessary. Show a formal column method in its expanded and/or shortened form where appropriate. Use concrete resources alongside this.



36	$3 6$	
$+25$	$2 5$	+
61	$1 1$	
1	$5 0$	
	$6 1$	



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<p>Column method - 3 digit and 2 digit numbers.</p> <p>Column method - 3 digit and 3 digit numbers.</p>	   <p>243 + 368</p>	 	 		
<p>Year 4</p> <p>Column method - regrouping (up to 4 digits)</p>	<p>Use base ten and place value counters within place value grids. Exchange ten ones for one ten etc. Begin with three digits, moving to four.</p>	<p>Represent the counters in a place value chart, circling when an exchange has been made.</p>  <p>Use part, part</p>	<p>Use the formal method when needed - making the appropriate decision as to when this is necessary, including with money and measure. Show alongside base ten.</p> 		



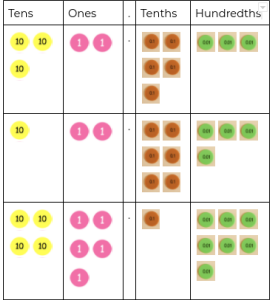
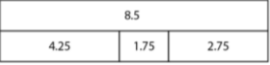
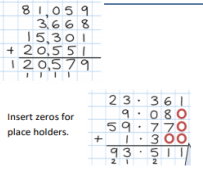
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		<p>whole models and bar models to support mental calculations.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td style="text-align: center;">?</td></tr> <tr><td style="text-align: center;">21</td><td style="text-align: center;">34</td></tr> </table> <p style="text-align: center;">$£1.37 + £2.45 = £3.82$</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td colspan="2" style="text-align: center;">£3.82</td></tr> <tr><td style="text-align: center;">£1.37</td><td style="text-align: center;">£2.45</td></tr> </table> $\begin{array}{r} + £1 = +3 \text{ p} \\ + £2 = +45 \text{ p} \\ \hline £ 3 \text{ } 82 \end{array}$?	21	34	£3.82		£1.37	£2.45	<p>$6,584 + 2,739 = 9,323$</p> $\begin{array}{r} 6,584 \\ + 2,739 \\ \hline 9,323 \end{array}$ <p>Solve missing digit problems and word problems.</p> <p>$7,000 - 2,648 = 6,999 - 2,647 = 4,352$</p> $\begin{array}{r} 7,000 \xrightarrow{-1} 6,999 \\ - 2,648 \xrightarrow{-1} 2,647 \\ \hline 4,352 \end{array}$																				
?																														
21	34																													
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<p>Year 5</p> <p>Column method - regrouping (more than 4 digits).</p>	<p>As Year 4.</p>	<p>Show exchanges using place value counters.</p>	<p>Use the formal column method for decimals and numbers with more than 4 digits.</p> $\begin{array}{r} 3517 \\ + 396 \\ \hline 3913 \end{array}$ <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td></td><td>Th</td><td>H</td><td>T</td><td>O</td></tr> <tr><td></td><td>4</td><td>3</td><td>5</td><td>6</td></tr> <tr><td>+</td><td>2</td><td>4</td><td>3</td><td>5</td></tr> <tr><td></td><td>6</td><td>7</td><td>9</td><td>1</td></tr> <tr><td></td><td></td><td></td><td></td><td>1</td></tr> </table>		Th	H	T	O		4	3	5	6	+	2	4	3	5		6	7	9	1					1		
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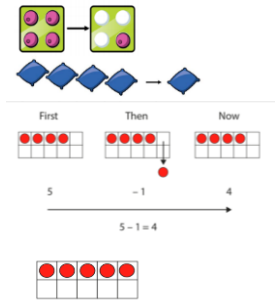
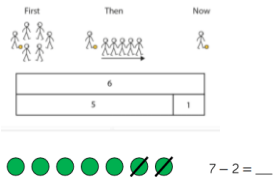
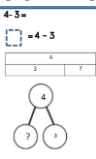


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<p>Use of place value counters for adding decimals.</p>	<p>Introduce decimal place value counters and model exchange.</p> 	<p>Represent decimal calculations using bar models.</p> 	<p> $\begin{array}{r} 2.55 \\ + 5.73 \\ \hline 8.28 \end{array}$ $2.55 + 5.73 = 8.28$ </p> <p> $\begin{array}{r} 72.8 \\ + 54.6 \\ \hline 127.4 \end{array}$ </p> <p> $\begin{array}{r} 23.59 \\ + 7.55 \\ \hline 31.14 \end{array}$ </p> <p>Solve missing number problems.</p> <table border="1" data-bbox="1142 580 1352 727"> <tr><td>?</td><td>4</td><td>?</td><td>3</td><td>?</td></tr> <tr><td>+</td><td>2</td><td>?</td><td>5</td><td>?</td><td>2</td></tr> <tr><td></td><td>7</td><td>8</td><td>5</td><td>2</td><td>9</td></tr> </table>	?	4	?	3	?	+	2	?	5	?	2		7	8	5	2	9					
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+	2	?	5	?	2																				
	7	8	5	2	9																				
<p>Year 6</p> <p>Column method - regrouping (several numbers).</p> <p>Abstract methods.</p> <p>Place value counters to be used for adding decimal numbers.</p>	<p>As Year 5</p>	<p>As Year 5</p>	<p>Use the formal column method for decimal numbers and several numbers.</p>  <p>Solve missing number problems.</p> <table border="1" data-bbox="1142 1193 1326 1308"> <tr><td>5</td><td>2</td><td>2</td><td>4</td><td>7</td><td>?</td></tr> <tr><td>+</td><td>3</td><td>?</td><td>5</td><td>9</td><td>0</td><td>4</td></tr> <tr><td></td><td>9</td><td>0</td><td>?</td><td>3</td><td>?</td><td>2</td></tr> </table>	5	2	2	4	7	?	+	3	?	5	9	0	4		9	0	?	3	?	2		
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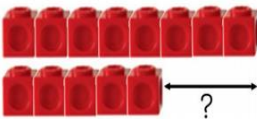
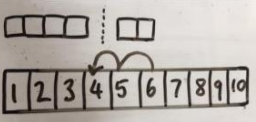
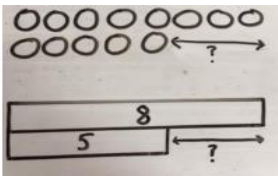
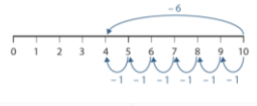


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Subtraction					
Objective and strategy	Concrete	Pictorial	Abstract	Sentence Stems for all year groups	Vocabulary for all year groups
<p>EYFS and Year 1</p> <p>Taking away ones.</p> <p>Counting back.</p>	<p>Physically take away and remove objects from a whole. Use a variety of objects including ten frames and Numicon.</p> <p>4 - 3 = 1</p>  <p>5 - 1 = 4</p>	<p>Draw the concrete resources they are using and cross out the correct amount. Show using the bar model.</p>  <p>7 - 2 = 2</p>	<p>Represent the calculation in the abstract using numerals, part, part, whole models and bar models.</p> 	<p>_____ is less than/smaller than/shorter than/lighter than</p> <p>I know _____ because _____</p> <p>There are less _____ than _____</p> <p>The difference between _____ and _____ is _____</p> <p>I know that _____ minus _____ is equal to _____ so _____ minus _____ is equal to _____</p> <p>If _____ minus _____ equals _____ then _____ minus _____ equals _____.</p>	<p>take away</p> <p>less than</p> <p>the difference</p> <p>subtract</p> <p>minus</p> <p>fewer</p> <p>decrease</p> <p>minuend</p> <p>subtrahend</p> <p>minuend - subtrahend = difference</p> <p>regrouping</p> <p>exchanging</p> <p>inverse</p>

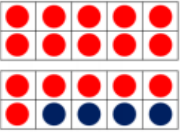
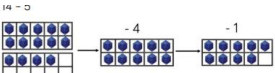
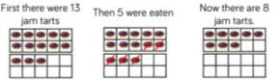
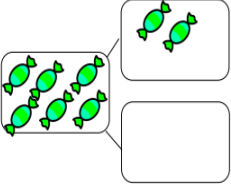
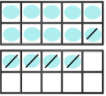

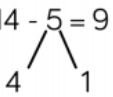
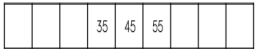


Arden Primary School Calculation Policy

<p>Find the difference.</p> <p>Represent and use number bonds and related subtraction facts within 20.</p>	 <p>Move objects away from the group as you count backwards.</p>  <p>Use cubes, Numicon, Cuisenaire Rods or other objects to calculate the difference.</p>  <p>Represent number bonds using ten frames and bead strings. Explore the</p>	 <p>Draw the cubes or other concrete resources they have used and begin to represent as a bar model.</p>  <p>Show number bonds using the part, part, whole model and</p>	 <p>"Put 8 in your head and count back 3..."</p> <p>Find the difference in the context of a problem, e.g. James has 12 cars and his brother has 7, how many more cars does James have than his brother?</p> <p>Record number bonds systematically and look for patterns in the inverse:</p>	<p>First...then...now...</p> <p>I've added _____ to the minuend and kept the subtrahend the same, so I must add _____ to the difference.</p> <p>Do I need to make an exchange?</p> <p>What has stayed the same?</p> <p>What has changed?</p>	<p>subitising - instantly recognising an amount.</p> <p>unitising -treating groups that contain or represent the same number of things as ones.</p>
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Arden Primary School Calculation Policy

<p>Make 10 using the ten frame.</p>	<p>subtraction facts.</p>  <p>14 - 5 on a ten frame = 14 - 4 - 1.</p>  	<p>counters. Use subtraction to find the missing number.</p>  <p>Present the ten frame pictorially, crossing out the numbers they have subtracted. Discuss what they did to first make ten.</p> 	<p>12 = 0 + 12, 12 - 0 = 12 12 = 1 + 11, 12 - 1 = 11 12 = 2 + 10, 12 - 2 = 10...</p> <p>Use the part, part, whole model to find the inverse calculation.</p>  <p>Show how to make ten by partitioning the subtrahend.</p> $14 - 5 = 9$  $14 - 4 = 10$ $10 - 1 = 9$		
<p>Year 2</p> <p>Subtract tens</p>	<p>Use base ten to explore patterns in adding and subtracting tens.</p>	<p>Look for patterns in the 100 square.</p>	<p>56 - 20 = 36 69 - 40 = 29</p> 		

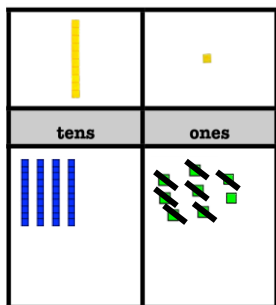
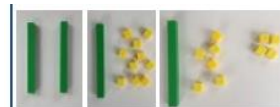
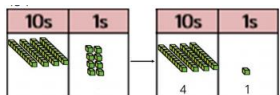


Arden Primary School Calculation Policy

Subtract one digit from two digits

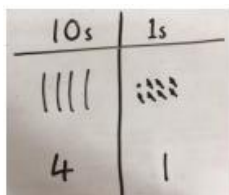
10 less	Number	10 more
	12	22
	37	

Use base ten and place value grids to represent the subtraction, exchanging ten for ones where necessary (begin with no exchange).



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Represent the base ten pictorially.



Represent the calculation on a number line, using partitioning and bridging to ten.



Show a formal column method in its expanded and/or shortened form where appropriate. Use alongside base ten.

$$\begin{array}{r} 48 \\ - 7 \\ \hline 41 \end{array}$$

$$\begin{array}{r} 408 \\ - 7 \\ \hline 401 \end{array}$$

$$48 - 7 = 41$$

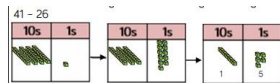
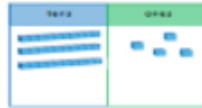


Arden Primary School Calculation Policy

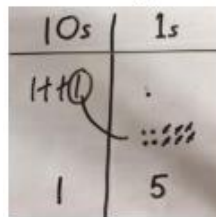
Subtract with two digits

Use base ten and place value grids to represent the subtraction. Exchanging tens for ones where necessary (begin with no exchange).

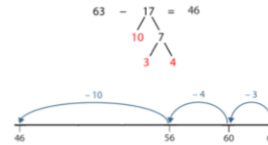
$$34 - 13$$



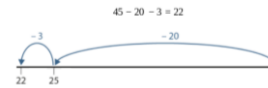
Represent the base ten pictorially, remembering to show the exchange.



Represent the calculation on a number line, using partitioning and bridging to ten.



Jump back on a number line in tens and ones.

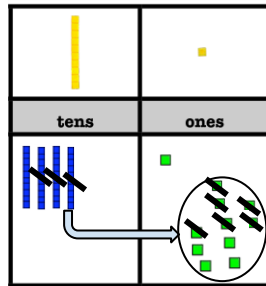


Show a formal column method alongside base ten in its expanded and/or shortened form where appropriate.

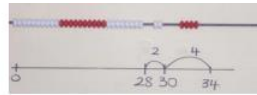
$$\begin{array}{r} \cancel{3}41 \\ - 26 \\ \hline 15 \end{array}$$



Arden Primary School Calculation Policy



Use a bead bar or bead strings to model counting to the next ten.



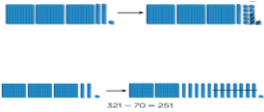
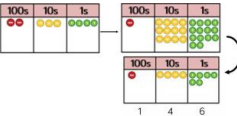
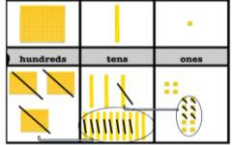
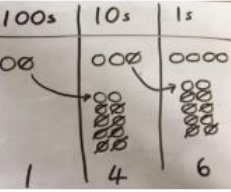

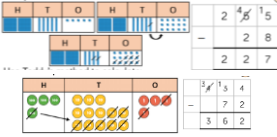

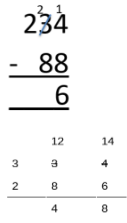

$$34 - 28$$

$$\begin{array}{r} 30 \quad 11 \\ 40 \quad 11 \\ \hline 20 \quad 6 \\ 10 \quad 5 \end{array}$$

$$41 - 26 = 15$$



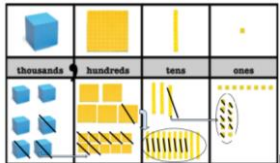



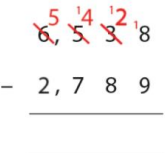
Arden Primary School Calculation Policy

<p>Year 3</p> <p>Column method three digits subtract one digit with and without regrouping.</p> <p>Column method three digits subtract two digits with and without regrouping.</p> <p>Column method three digits subtract three digits with and without regrouping.</p>	<p>Represent the calculation using base ten or place value counters and place value grids. Begin with TO -TO from year two then build up to three digit numbers. First examples involve no regrouping, later begin regrouping using apparatus.</p>   <p>234 - 88</p> 	<p>Represent the place value counters and base ten pictorially remembering to show what has been exchanged.</p> <p>Represent calculations as bar models and part, part, whole models.</p>   <table border="1" data-bbox="824 1238 1055 1289"> <tr> <td colspan="2">391</td> </tr> <tr> <td>186</td> <td>?</td> </tr> </table>	391		186	?	<p>Show a formal column method alongside base ten in its expanded and/or shortened form where appropriate.</p>   $\begin{array}{r} 234 \\ - 88 \\ \hline 146 \end{array}$  		
391									
186	?								

Some content taken/adapted from:
 DfE National Curriculum
 NCETM
 White Rose Maths

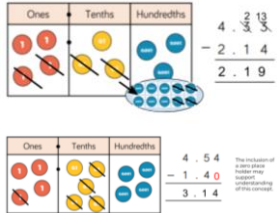
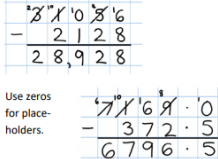
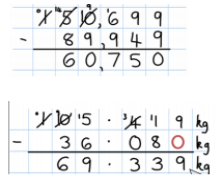


Arden Primary School Calculation Policy

<p>Year 4</p> <p>Column method with regrouping. (up to 4 digits)</p>	<p>Represent the calculation using base ten or place value counters and place value grids. Begin with HTO - HTO from year three then build up to four digit numbers. First examples involve no regrouping, later begin regrouping using apparatus.</p> 	<p>Represent the place value counters and base ten pictorially remembering to show what has been exchanged.</p> <p>Represent calculations as bar models and part, part, whole models.</p>  	<p>Show a formal column method alongside base ten in its expanded form if necessary, with all children using the shortened form where appropriate.</p> <p>Introduce decimal subtraction through the context of money.</p>  <p>6,538 - 2,789 = 3,749</p> 		
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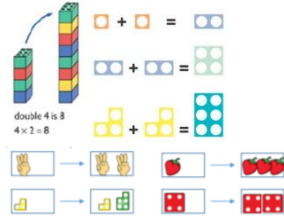
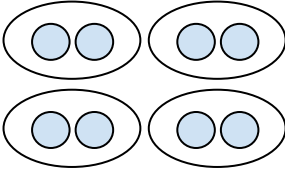
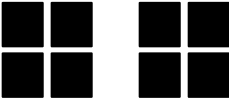
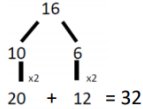


Arden Primary School Calculation Policy

<p>Year 5</p> <p>Column method with regrouping.</p> <p>Abstract for whole numbers.</p> <p>Start with place value counters for decimals- with the same amount of decimal places.</p>	<p>As Year 4 - at least 4 digits.</p> 	<p>As Year 4 - at least 4 digits.</p>	<p>Subtract with decimal values, including mixtures of integers and decimals and aligning the decimal point.</p> 		
<p>Year 6</p> <p>Column method with regrouping.</p> <p>Abstract methods.</p> <p>Place value counters for decimals- with different amounts of decimal places.</p>	<p>As Year 5.</p>	<p>As Year 5.</p>	<p>Subtract with increasingly large and more complex numbers and decimal values.</p> <p>Make an appropriate choice as to method depending on the complexity/size of the numbers.</p> 		

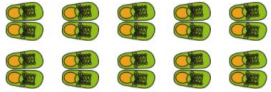











Arden Primary School Calculation Policy

Multiplication					
Objective and strategy	Concrete	Pictorial	Abstract	Sentence Stems for all year groups	Vocabulary for all year groups
<p>EYFS and Year 1</p> <p>Recognising and making equal groups.</p> <p>Doubling.</p>	<p>Use cubes and other objects in the classroom to make and recognise equal groups.</p>  <p>Use manipulatives including cubes and Numicon to demonstrate doubling.</p>  <p>Count the groups of objects in 10s, 2s,</p>	<p>Draw objects to represent the equal groups found.</p>  <p>Double 4 is 8.</p>  <p>Represent the</p>	<p>Represent the equal groups as 4 groups of 2 or $4 \times 2 = 8$.</p> <p>Partition a number then double each part before recombining it back together.</p>  <p>Count in multiples of</p>	<p>There are ____ ____ in ____ _____.</p> <p>The groups are equal because there are the same number of ____ in each group.</p> <p>There are ____ equal groups of ____. There are ____ in each group. There are ____ groups of ____.</p> <p>The product of ____ and ____ is ____.</p> <p>A times b can represent a groups of b. It can also represent b groups of a.</p>	<p>double</p> <p>times</p> <p>multiplied by</p> <p>the product of</p> <p>groups of</p> <p>lots of</p> <p>equal groups</p> <p>factor</p> <p>inverse</p> <p>factor x factor = product</p> <p>commutative law - a sum or product can be calculated in any order (e.g. $ab = ba$).</p>

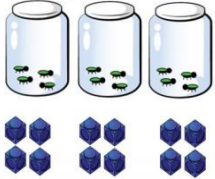
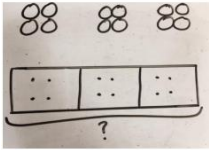
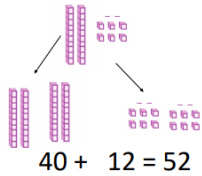
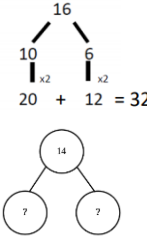


Arden Primary School Calculation Policy

<p>Counting in multiples.</p>	<p>5s becoming more efficient - begin to use arrays.</p> <p>Count pairs of shoes.</p>  <p>Count the petals in fives and 'high fives'.</p>   <p>Use ten frames and hands to count in tens.</p>   <p>Recognise the equal groups and describe how many are in each group -</p>	<p>counting with diagrams using efficient organisation - begin to use arrays.</p>   <p>Look for patterns on the Gattegno Chart.</p>  <p>Use a bar model to represent the calculation.</p> $6 \times 5 = 30$  <p>Represent the practical resources</p>	<p>10, 2 and 5 out loud.</p> <p>Write the sequences of numbers.</p> <p>10, 20, 30, 40, 50...</p> <p>2, 4, 6, 8, 10...</p> <p>5, 10, 15, 20, 25...</p>  <p>Write the number sentence to describe the resources used:</p>	<p>_____ is a factor so we can use the _____ times tables.</p> <p>I know that double _____ is _____, so half of _____ is _____.</p> <p>Products in the _____ times tables are also in the _____ times tables.</p> <p>If _____ is a factor of _____ then it is also a factor of _____.</p> <p>Both factors are the same, so we can also write this as _____ squared is equal to _____.</p> <p>The _____ is _____ times the length/weight/height of the _____.</p> <p>If I multiply one</p>	<p>associative law - we can group numbers in any order when adding or multiplying (e.g. $(a + b) + c = (b + c) + a$)</p> <p>distributive law - $a \times (b + c) = (a \times b) + (a \times c)$</p> <p>multiple</p> <p>prime number</p> <p>square number</p> <p>cube number</p> <p>composite number</p> <p>highest common factor</p> <p>subitising - instantly recognising an amount.</p>
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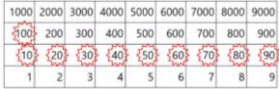
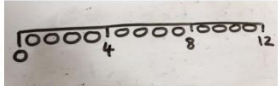
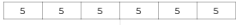
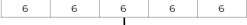
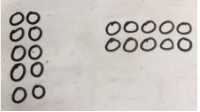


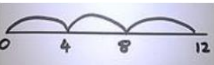

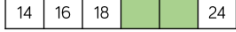
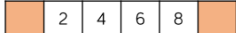


Arden Primary School Calculation Policy

<p>Repeated addition.</p>	<p>'there are three equal groups, with four in each group.'</p> 	<p>in a picture and use a bar model.</p> 	<p>$4 + 4 + 4 = 12$ $3 \times 4 = 12$</p>	<p>factor by _____, then I must divide the other factor by _____ for the product to stay the same.</p> <p>_____ is a factor of _____ because _____ x _____ = _____.</p>	<p>unitising -treating groups that contain or represent the same number of things as ones.</p>
<p>Year 2</p> <p>Doubling</p> <p>10, 2, 5 times tables.</p>	<p>Use base ten to show the partitioned approach to doubling.</p>  <p>$40 + 12 = 52$</p>	<p>Draw pictures, representations and the part, part, whole model to show the partitioned approach to doubling.</p>  <p>Use number lines, counting sticks and bar models to show representations of counting in</p>	<p>Partition and recombine, using models to support.</p> <p>$16 \times 2 = 10 \times 2 + 6 \times 2$</p> <p>Count in multiples of a number out loud and write the sequence of numbers. Write the number sentence for</p>	<p>_____ is a multiple of _____ because _____ x _____ = _____.</p> <p>Do I need to make an exchange?</p> <p>What has stayed the same?</p> <p>What has changed?</p>	



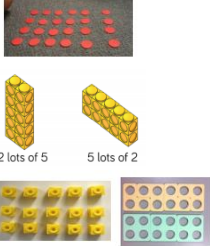
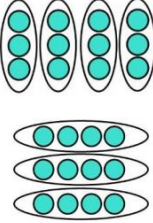


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<p>Arrays- showing commutative multiplication and inverse</p>	<p>frames to represent the numbers and see the sequence.</p>     <p>Create arrays using counters, cubes and Numicon, recognising that the array represents different equations and that</p>	<p>multiples. Recognise the pattern in a Gattegno Chart.</p>    <p>$6 \times 5 = 30$ Or</p>  <p>$5 \times 6 = 30$</p> <p>Represent arrays pictorially.</p> 	<p>the times tables facts. Number lines can support thinking.</p> <p>0, 5, 10, 15, 20...</p> <p>$3 \times 5 = 15$</p>       <p>Explore patterns in the times tables facts and use these to decide if a number is a multiple of 2, 5, 10. Use the array to write a range of</p>		
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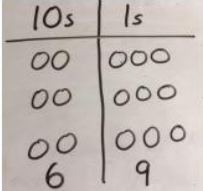
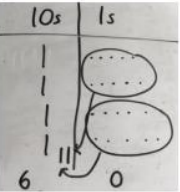



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	<p>multiplication is commutative.</p>  <p>2 lots of 5 5 lots of 2</p>	 <p>Represent the inverse as 'fact families.'</p>  <p> <input type="checkbox"/> × <input type="checkbox"/> = <input type="checkbox"/> <input type="checkbox"/> × <input type="checkbox"/> = <input type="checkbox"/> <input type="checkbox"/> ÷ <input type="checkbox"/> = <input type="checkbox"/> <input type="checkbox"/> ÷ <input type="checkbox"/> = <input type="checkbox"/> </p>	<p>calculations including repeated addition and inverse calculations. Inverse to be taught alongside division .</p> <p> $10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $5 + 5 = 10$ $10 \div 5 = 2$ $5 = 10 \div 2$ </p>																																																				
<p>Year 3</p> <p>3, 4 and 8 times tables.</p>	<p>Represent the 3, 4 and 8 times tables using objects, cubes and counters. Record the multiplication statements alongside this.</p> <p> _ + _ + _ + _ + _ = _ _ × _ = _ </p>  <p>Show the multiplication facts as arrays and find the four facts (x</p>	<p>Count in multiples of 3, 4 8 on a drawn number line and recognise patterns on a 100 square.</p> <table border="1" data-bbox="831 999 1099 1145"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> </table> <p>Represent the calculations in a bar model.</p>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	<p>Record multiplication facts as repeated addition and in their inverse form. Use arrays.</p> <p>Explore patterns in the times tables facts and use these to decide if a number is a multiple of 3, 4, 8. Recognise the relationship between 2, 4, 8 times tables.</p>		
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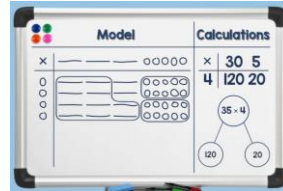
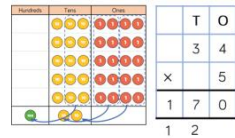
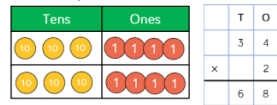
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<p>Multiply TO by \times using the grid and short methods.</p>	<p>and \div) that go with it..</p>  <p>Use place value counters and/or base ten apparatus to represent the multiplication calculation.</p> <table border="1" data-bbox="521 678 672 805"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table> <p>21×3</p> <p>Show alongside a grid to explore the use of the grid method.</p> <table border="1" data-bbox="515 1109 795 1268"> <thead> <tr> <th>Model</th> <th>Calculations</th> </tr> </thead> <tbody> <tr> <td></td> <td> $\begin{array}{r} \times 20 \ 3 \\ 6 \ 120 \ 18 \end{array}$ </td> </tr> </tbody> </table>	Tens	Ones							Model	Calculations		$\begin{array}{r} \times 20 \ 3 \\ 6 \ 120 \ 18 \end{array}$	<p></p> <p>$5 \times 3 = 15$</p> <p>Represent the counters and/or base ten pictorially.</p>  <p>23×3</p>  <p>15×4</p> <p>Represent the grid method pictorially.</p>	<p>Count in 3, 4, 8 using counting sticks and other resources.</p> <p>Record informally using mental methods and partitioning (grid method), leading to expanded column method and finally the column method as appropriate.</p> <table border="1" data-bbox="1131 750 1265 813"> <tbody> <tr> <td>\times</td> <td>20</td> <td>3</td> </tr> <tr> <td>6</td> <td>120</td> <td>18</td> </tr> </tbody> </table>  <table border="1" data-bbox="1131 1045 1209 1141"> <tbody> <tr> <td>23</td> </tr> <tr> <td>\times 6</td> </tr> <tr> <td>138</td> </tr> <tr> <td>11</td> </tr> </tbody> </table>	\times	20	3	6	120	18	23	\times 6	138	11		
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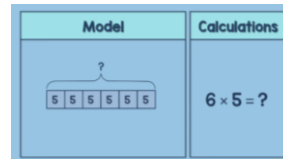


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When the children are unitising confidently, move to the use of place value counters and the short method.




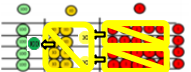
Represent word problems using a bar model.



Muffins come in boxes of 5, Peter buys 6 boxes of muffins. How many muffins does Peter buy altogether?



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<p>Year 4</p> <p>6, 7, 9, 11 and 12 times tables.</p> <p>Multiply TO and HTO by O using column multiplication.</p>	<p>Represent the 6, 7, 9, 11, 12 times tables using objects, cubes and counters. Record the multiplication statements alongside this. Show the 11 and 12 times tables using base ten.</p>  <p>Recap the grid method from year 3 using place value counters.</p>  <p>Base ten and place value counters can be used alongside the short and expanded column methods.</p>	<p>Count in multiples of 6, 7, 9, 11, 12 on a drawn number line and recognise patterns on a 100 square.</p> <table border="1" data-bbox="824 422 1108 710"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> <tr><td>51</td><td>52</td><td>53</td><td>54</td><td>55</td><td>56</td><td>57</td><td>58</td><td>59</td><td>60</td></tr> <tr><td>61</td><td>62</td><td>63</td><td>64</td><td>65</td><td>66</td><td>67</td><td>68</td><td>69</td><td>70</td></tr> <tr><td>71</td><td>72</td><td>73</td><td>74</td><td>75</td><td>76</td><td>77</td><td>78</td><td>79</td><td>80</td></tr> <tr><td>81</td><td>82</td><td>83</td><td>84</td><td>85</td><td>86</td><td>87</td><td>88</td><td>89</td><td>90</td></tr> <tr><td>91</td><td>92</td><td>93</td><td>94</td><td>95</td><td>96</td><td>97</td><td>98</td><td>99</td><td>100</td></tr> </table> <p>Represent the place value counters pictorially. Draw the counters using circles or colours to represent the different values.</p> <table border="1" data-bbox="828 1117 1097 1197"> <thead> <tr><th>Hundreds</th><th>Tens</th><th>Ones</th></tr> </thead> <tbody> <tr><td>●●●</td><td>●●●●</td><td>●●●●●●</td></tr> </tbody> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	Hundreds	Tens	Ones	●●●	●●●●	●●●●●●	<p>Explore patterns in the times tables facts and use these to decide if a number is a multiple of 6, 7, 9, 11, 12. Recognise the relationship between 3, 6, 9 times tables.</p> <p>Count in 6, 7, 9, 11, 12 using counting sticks and other resources.</p> <p>Represent as a grid method with formal column addition to find the final answer.</p> <table border="1" data-bbox="1153 885 1288 949"> <tr><td>x</td><td>100</td><td>20</td><td>6</td></tr> <tr><td>4</td><td>400</td><td>80</td><td>24</td></tr> </table> <pre data-bbox="1153 965 1198 1045"> 400 80 + 24 --- 504 </pre> <p>Use the expanded and short column method with TO x O then HTO by O alongside place value counters.</p>	x	100	20	6	4	400	80	24		
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	<p>321 × 3 = 963</p> <p>521 × 3 = 1,563</p>		<p>367 × 4 = 1,468</p>														
<p>Year 5</p> <p>Column multiplication up to 4 digit numbers multiplied by 1 or 2 digits.</p>	<p>Recap learning from Year 4 using place value counters and base ten. Move towards TO x TO, ThHTO x O, ThHTO x TO, HTO x TO.</p>	<p>Use the grid method where necessary to support the understanding of the column multiplication method.</p> <table border="1" data-bbox="840 1045 1019 1133"> <tr><td>x</td><td>100</td><td>60</td><td>7</td></tr> <tr><td>80</td><td>8000</td><td>4800</td><td>560</td></tr> <tr><td>6</td><td>600</td><td>360</td><td>42</td></tr> </table> <p>8000 4800 600 + 560 360 42 14362 21</p>	x	100	60	7	80	8000	4800	560	6	600	360	42	<p>Multiply using the column method for 4 digit numbers x 1 or 2 digits.</p>		
x	100	60	7														
80	8000	4800	560														
6	600	360	42														

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Model		Calculations	
\times		13	
		$\times 15$	
		150	
		300	
		$+ 100$	
		195	

Thousands	Hundreds	Tens	Ones	Tn	H	T	O
				1	0	2	3

Support the understanding of decimal multiplication using place value counters before moving into a formal method.

$4 \times 7 = 28$	$4 \times 0.7 = 2.8$
$4 \times 7 \text{ ones} = 28 \text{ ones}$	$4 \times 7 \text{ tenths} = 28 \text{ tenths}$

		3	2	5	0	
\times					2	6
	1	9	5	0	0	$(3,250 \times 6)$
	6	5	0	0	0	$(3,250 \times 20)$
	8	4	5	0	0	

Show decimal multiplication alongside its non-decimal counterpart so that children can see the relationship. Ensure sufficient coverage of $\div 10/100/1000$ first.

5.7	$\times 3$	$=$	17.1
$\times 10 \downarrow$			$\uparrow \div 10$
57	$\times 3$	$=$	171

5	7
\times	3
1	7
1	7
2	

57	5.7
$\times 3$	$\times 3$
171	17.1
2	2

2	.	4	6
\times			3
7	.	3	8
1		1	

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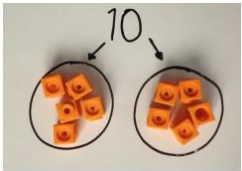

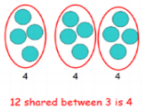
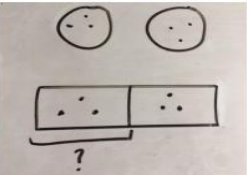
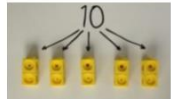

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<p>Year 6</p> <p>Column multiplication with multi-digit up to 4 digits by a 2 digit number.</p>	<p>As Year 5</p>	<p>As Year 5</p>	<p>As Year 5 plus multiplying decimals up to 2dp by a single digit.</p> $\begin{array}{r} 3.19 \\ \times 8 \\ \hline 25.52 \end{array}$		
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Division					
Objective and strategy	Concrete	Pictorial	Abstract	Sentence Stems for all year groups	Vocabulary for all year groups
<p>EYFS and Year 1</p> <p>Sharing objects into groups.</p>	<p>Share objects into equal groups using a range of materials.</p>   	<p>Use pictures or shapes to share quantities.</p>   	<p>6 shared between 2 equals 3 10 shared between 5 equals 2</p>	<p>_____ divided into _____ groups of _____</p> <p>_____ divided between _____</p> <p>_____ divided by _____.</p> <p>There are _____ groups and a remainder of _____.</p> <p>_____ is a multiple of _____, so when it is divided into groups of _____, there is no remainder.</p> <p>If I multiply the dividend by _____, I must multiply the divisor by _____ for the quotient to stay the same.</p>	<p>share</p> <p>group</p> <p>divide</p> <p>divided by</p> <p>half</p> <p>dividend</p> <p>divisor</p> <p>quotient</p> <p>dividend ÷ divisor = quotient</p> <p>subitising - instantly recognising an amount.</p> <p>unitising -treating groups that contain or represent the</p>
<p>Division as grouping</p>	<p>Use cubes, counters and other objects to make groups of... e.g. Put 10 cubes into groups of 2.</p> 	<p>Draw the cubes, counters and other objects to represent the calculation.</p> 	<p>10 put into groups of 2 equals 5</p>		

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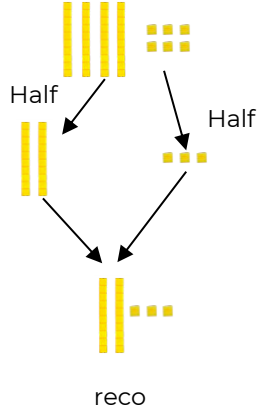
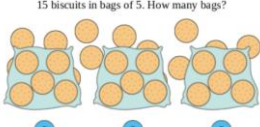
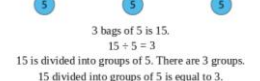
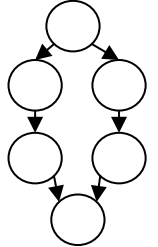
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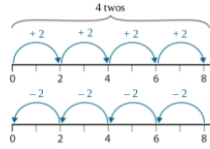
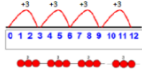
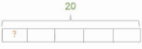
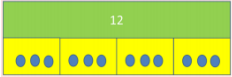
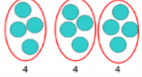
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<p>Year 2</p> <p>Halving</p> <p>Division as grouping within the 2, 5 and 10 times tables. .</p>	<p>Use base ten to show the partitioned approach to halving.</p>  <p>reco</p> <p>Use cubes, counters and other objects to make equal groups of... e.g. Put 10 cubes into groups of 2.</p>  <p>15 biscuits in bags of 5. How many bags?</p>  <p>3 bags of 5 is 15. 15 ÷ 5 = 3 15 is divided into groups of 5. There are 3 groups. 15 divided into groups of 5 is equal to 3.</p>	<p>Draw pictures, representations and the part, part, whole model to show the partitioned approach to halving.</p>  <p>Represent the division on a number line or bar model, including the use of repeated subtraction.</p>	<p>Partition and recombine, using models to support.</p> $46 \div 2 = 40 \div 2 + 6 \div 2$ $= 20 + 3 = 23$ $15 \div 3 = 5$ $15 - 3 - 3 - 3 - 3 - 3$ <p>Divide 15 into 3 groups, how many in each group?</p>	<p>_____ is a factor of _____ because _____ ÷ _____ = _____.</p> <p>_____ is a multiple of _____ because _____ ÷ _____ = _____.</p> <p>Do I need to make an exchange?</p> <p>What has stayed the same?</p> <p>What has changed?</p>	<p>same number of things as ones.</p>
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<p>Division as sharing within the 2, 5 and 10 times tables.</p>	<p>Share objects into equal groups using a range of materials.</p> <p>Share the 12 cubes equally into the two boxes.</p> <p>There are ___ cubes altogether. There are ___ boxes. There are ___ cubes in each box.</p>  <p>Represent the division as an array and notice the connection between multiplication and division.</p> <p>10 children, 30 meatballs. How many each?</p>  <p>$30 \div 10 = 3$</p> <p>3 tens is 3 each.</p>	 <p>8 is divided into groups of 2. There are 4 groups. $8 \div 2 = 4$ 8 divided into groups of 2 is equal to 4. So, 4 children get balloons.</p>   <p>Use pictures or shapes to share quantities. Use bar modelling to show and support understanding.</p>  <p>$12 \div 4 = 3$</p>  <p>12 shared between 3 is 4</p>	<p>$15 \div 5 = 3$</p>		
<p>Year 3</p> <p>Division of TO by O including examples with a remainder.</p>	<p>Continue the work begun in Year 2 with arrays, sharing and grouping</p>	<p>Continue the work begun in Year 2 with arrays, sharing and grouping</p>	<p>Continue the work begun in Year 2 with arrays, sharing and</p>		

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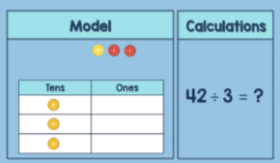
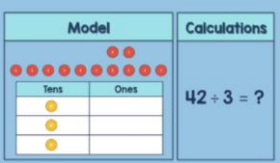
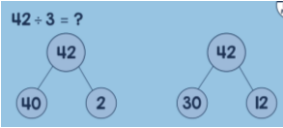
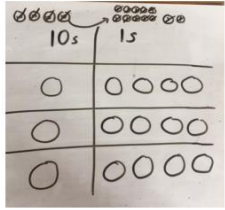
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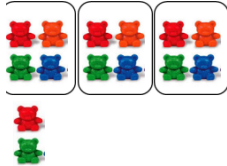
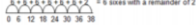
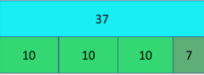



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	<p>within the 3, 4 and 8 times tables.</p> <p>Use place value counters to show the division. Begin with the dividend, which is then split into the appropriate number of groups according to the divisor.</p>  <p>Make an exchange where this is necessary.</p>  <p>Continue sharing according to the divisor and</p>	<p>within the 3, 4 and 8 times tables.</p> <p>Show how the number has been partitioned in order to carry out the division. Use a part, part, whole model.</p>  <p>Represent the place value counters pictorially.</p>  <p>Use number lines to support understanding and show where there</p>	<p>grouping within the 3, 4 and 8 times tables.</p> <p>Understand the calculations that have been carried out with the place value counters and represent as number sentences.</p> <p>$42 \div 3$ $42 = 30 + 12$ $30 \div 3 = 10$ $12 \div 3 = 4$ $10 + 4 = 14$</p> <p>Complete written divisions, showing the remainder using r.</p> <p>$28 \div 5 = 5 \text{ r } 3$</p>		
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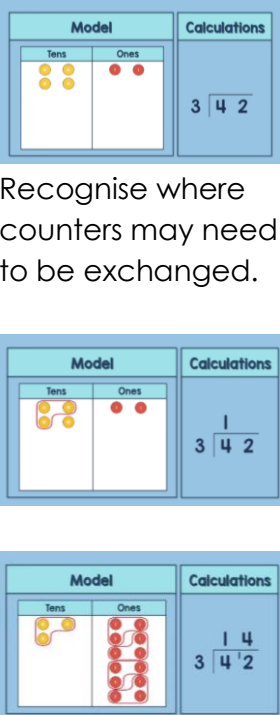
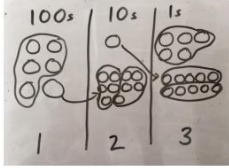
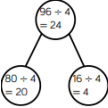
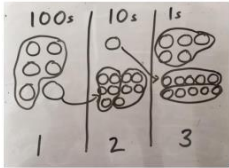


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	<p>represent the calculation as a number sentence.</p> <table border="1" data-bbox="517 336 795 502"> <thead> <tr> <th colspan="2">Model</th> <th>Calculations</th> </tr> </thead> <tbody> <tr> <td>Tens</td> <td>Ones</td> <td rowspan="3">$42 \div 3 = 14$</td> </tr> <tr> <td>●</td> <td>●●●●</td> </tr> <tr> <td>●</td> <td>●●●●</td> </tr> </tbody> </table> <p>Divide objects between groups and see how many are left over to illustrate the concept of 'remainders'.</p>  <p>$14 \div 3 = 4 \text{ r } 2$</p>	Model		Calculations	Tens	Ones	$42 \div 3 = 14$	●	●●●●	●	●●●●	<p>might be a remainder.</p> <p><small>Example with remainder $28 \div 6$</small></p>  <p>Draw dots and group them to clearly show where there might be a remainder. Represent on a bar model.</p>  			
Model		Calculations													
Tens	Ones	$42 \div 3 = 14$													
●	●●●●														
●	●●●●														
<p>Year 4</p> <p>Short division of HTO by O including remainders..</p>	<p>Use place value counters to divide TO and HTO by O, including where there is a remainder. Show alongside the short</p>	<p>Represent the place value counters pictorially.</p>	<p>Use known multiplication facts to recognise when a division calculation will have a remainder and make a prediction.</p>												



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	<p>division method.</p>  <p>Recognise where counters may need to be exchanged.</p>	 <p>Show the calculation as a part, part, whole model.</p> 	<p>Use the short division strategy, showing clearly any remainders.</p> $\begin{array}{r} 123 \\ 5 \overline{) 615} \end{array}$		
<p>Year 5</p> <p>Short division up to ThHTO by O including remainders.</p>	<p>Use place value counters to divide TO, HTO, ThHTO and decimals by O, including where there is a remainder. Show alongside the short division method.</p>	<p>Represent the place value counters pictorially.</p> 	<p>Use the short division strategy for whole numbers and decimals, showing clearly any remainders.</p>		

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			$\begin{array}{r} 17 \\ 5 \overline{) 88} \\ \underline{5} \\ 35 \\ \underline{35} \\ 0 \end{array}$ $\begin{array}{r} 17 \\ 5 \overline{) 88} \\ \underline{5} \\ 35 \\ \underline{35} \\ 0 \end{array}$ <p>85 ones \div 5 = 17 ones so 85 hundredths \div 5 = 17 hundredths $0.85 \div 5 = 0.17$</p>		
<p>Year 6</p> <p>Short division.</p> <p>Long division up to 4 digits by a 2 digit number (including decimals).</p>	<p>Short division as Year 5 plus use place value counters to write the remainder as a decimal or fraction.</p> <p>Long division, e.g. $2544 \div 12$.</p> <p>We can't group 2 thousands into groups of 12 so we</p>	<p>Represent the place value counters pictorially.</p>	<p>Use the short division strategy for whole numbers and decimals, showing clearly any remainders, writing them in their decimal or fractional form.</p> <p>Show remainders in three forms:</p> $\begin{array}{r} 31 \\ 2 \overline{) 62} \\ \underline{62} \\ 0 \end{array} \text{ r1}$ $\begin{array}{r} 31 \\ 2 \overline{) 62} \\ \underline{62} \\ 0 \end{array} \text{ } \frac{1}{2}$ $\begin{array}{r} 31.5 \\ 2 \overline{) 62.5} \\ \underline{62} \\ 50 \\ \underline{50} \\ 0 \end{array}$		

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
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	<p>will exchange them.</p> <table border="1" data-bbox="517 336 792 459"> <thead> <tr> <th>1000s</th> <th>100s</th> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td>25</td> <td>44</td> <td></td> </tr> </tbody> </table> $\begin{array}{r} 02 \\ 12 \overline{)2544} \\ \underline{24} \\ 1 \end{array}$ <p>We can group 25 hundreds into groups of 12, leaving one hundred remaining.</p> <table border="1" data-bbox="517 772 792 895"> <thead> <tr> <th>1000s</th> <th>100s</th> <th>10s</th> <th>1s</th> </tr> </thead> <tbody> <tr> <td></td> <td>14</td> <td>44</td> <td></td> </tr> </tbody> </table> $\begin{array}{r} 021 \\ 12 \overline{)2544} \\ \underline{24} \\ 14 \\ \underline{12} \\ 2 \end{array}$ <p>After exchanging the hundred, we have 14 tens. We can group 12 tens into a group of 12</p>	1000s	100s	10s	1s		25	44		1000s	100s	10s	1s		14	44			<p>Long division for 4 digits divided by 2 digits.</p> $\begin{array}{r} 0212 \\ 12 \overline{)2544} \\ \underline{24} \\ \text{inder. } 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$ <p>Use knowledge of factors to simplify long division calculations into two short division calculations.</p> <p>E.g. $2364 \div 27 = (2364 \div 9) \div 3 = 87 \text{ r } 5$.</p> <p>Use knowledge of multiples to support 4 digit by 2 digit division.</p>		
1000s	100s	10s	1s																		
	25	44																			
1000s	100s	10s	1s																		
	14	44																			



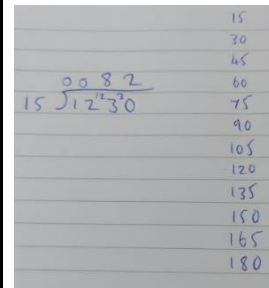
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which leaves 2
tens.

1000s	100s	10s	1s
			

$$\begin{array}{r} 0212 \\ 12 \overline{)2544} \\ \underline{24} \\ \text{inder. } 14 \\ \underline{12} \\ 24 \\ \underline{24} \\ 0 \end{array}$$









After exchanging
the two tens, we
have 24 ones. We
can group 24 ones
into 2 groups of 12
which leaves no
remainder.



15
30
45
60
75
90
105
120
135
150
165
180

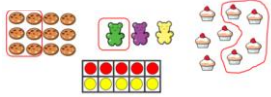

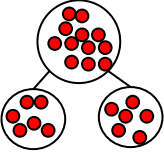

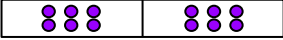

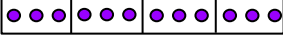
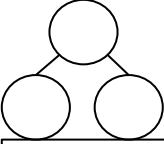

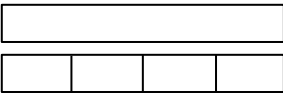


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Fractions (calculation only)					
Objective and strategy	Concrete	Pictorial	Abstract	Sentence Stems for all year groups	Vocabulary for all year groups
<p>EYFS and Year 1</p> <p>Find half of an object, shape or quantity, recognising that half is one of two equal parts.</p> <p>Find a quarter of an object, shape or quantity, recognising that a quarter is one of four equal parts.</p>	<p>Use familiar objects and counters.</p>   <p>Use familiar objects and counters.</p>  <p>There are ___ cakes. There is ___ cake in each quarter. A quarter of ___ is ___</p>  <p>There are ___ sweets. There are ___ sweets in each quarter. A quarter of ___ is ___</p>  <p>There are ___ peaches. There are ___ peaches in each quarter. A quarter of ___ is ___</p>	<p>Recognise halves and quarters in drawn shapes.</p>   <p>Draw the counters they have split into half.</p> 	<p>None at this stage. Children will just use the words half and quarter not the notation $\frac{1}{2}$ or $\frac{1}{4}$.</p>	<p>This is a whole ____ because I have all of it.</p> <p>There are ____ in the whole group.</p> <p>There are ____ in this part of the group.</p> <p>____ is a whole, ____ is a part and ____ is a part.</p> <p>The whole is</p>	<p>numerator</p> <p>denominator</p> <p>tenth</p> <p>hundredth</p> <p>proper fraction</p> <p>improper fraction</p> <p>equivalent fraction</p> <p>mixed number</p>

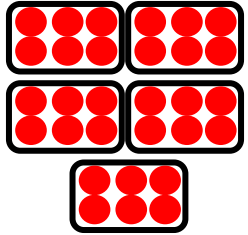

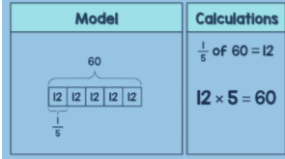


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<p>Year 2</p> <p>Find $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$, $\frac{3}{4}$ of a length, shape, set or quantity, recognising that the parts have to be equal.</p> <p>Find the non-unit fraction three quarters.</p>	<p>Use familiar objects and counters to show the fractions.</p>  <p>Share counters into four equal parts and count three parts.</p> 	<p>Begin to represent the fractions in bar models and part, part, whole models.</p>      <p>Find three quarters using bar models.</p>	<p>Use the notation for fractions, e.g. $\frac{1}{2}$ of 12 is 6 and $\frac{1}{3}$ of 15 is 5.</p> <p>Represent the bar model and part, part, whole model with numerals.</p>   	<p>divided into ____ equal parts.</p> <p>____ of the parts has been shaded.</p> <p>____ can be written as ____.</p> <p>I say __ . __ but I think __ wholes and __ tenths.</p> <p>____ is between ____ and ____.</p> <p>____ is the previous whole number/tenth/hundredth and ____ is the next whole number/tenth/hundredth.</p> <p>____ is 10/100/1000 times</p>	<p>common denominator</p> <p>vinculum (fraction bar)</p> <p>integer</p> <p>common denominator</p>
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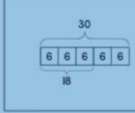
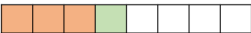



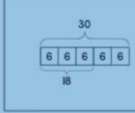



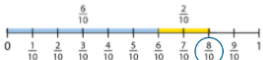
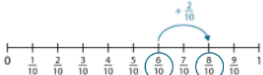
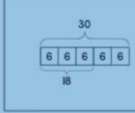





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<p>Year 3</p> <p>Find unit and non-unit fractions of amounts.</p>	<p>Separate counters into equal groups, relating to division. $30 \div 5 = 6$ therefore $\frac{1}{5}$ of 30 = 6. $\frac{3}{5}$ of 30 = 18.</p>  <p>Begin to show the counters within the bar model diagram. Counting more sections when calculating a non-unit fraction.</p>  <p>When working with larger numbers, use place value counters to calculate.</p>	<p>Show the bar model using counters or figures, alongside the abstract calculation, varying the question type to enable deeper understanding. E.g. $\frac{1}{5}$ of a number is 12, what is the number?</p>  <p>Recognise that to find a non-unit fraction of an amount, the same bar model can be used - with more sections being counted. Show alongside the abstract calculation. E.g. Peter has 30</p>	<p>$\frac{1}{5}$ of 60 = 12 $60 \div 5 = 12$</p> <p>$30 \div 5 = 6$ $6 \times 3 = 18$ $\frac{3}{5}$ of 30 = 18</p> <p>Once the bar model has been explored, understand the abstract concept as "divide by the denominator and multiply by the numerator."</p>	<p>bigger than ____.</p> <p>If ____ is the whole, then ____ is part of the whole.</p> <p>The denominator is ____ because the whole is divided into ____ equal parts.</p> <p>The numerator is ____ because ____ parts are shaded.</p> <p>The whole has been divided into ____ equal parts. ____ of the parts have been shaded; that is ____ of the whole.</p> <p>There are ____ parts between zero and one, that means we are counting in units of ____.</p>	
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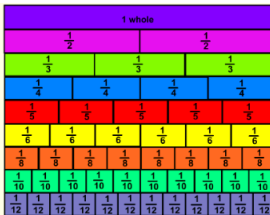


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<p>Add and subtract fractions with the same denominator.</p>	<p>E.g. find $\frac{1}{4}$ of 84 = 21, $\frac{3}{4}$ of 84 = 63.</p>  <p>Use paper strips and circles to explore adding and subtracting fractions and show as number sentences.</p> 	<p>sweets. He eats $\frac{3}{5}$ of the sweets. How many sweets does he eat?</p> <table border="1" data-bbox="824 352 1104 512"> <thead> <tr> <th>Model</th> <th>Calculations</th> </tr> </thead> <tbody> <tr> <td></td> <td>$\frac{1}{5}$ of 30 = 6 $30 \div 5 = 6$ $6 \times 3 = 18$ $\frac{3}{5}$ of 30 = 18</td> </tr> </tbody> </table> <p>Use bar models to represent the paper strips and perform the calculations.</p>  <p>We can use this model to calculate $\frac{3}{8} + \frac{1}{8} = \frac{4}{8}$</p> <p>Cross out the sections of the bar that are being subtracted.</p> <table border="1" data-bbox="831 1059 1099 1155"> <thead> <tr> <th>First</th> <th>Then</th> <th>Now</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> <td></td> </tr> <tr> <td>$\frac{5}{7}$</td> <td>$\frac{5}{7} - \frac{2}{7}$</td> <td>$\frac{3}{7}$</td> </tr> </tbody> </table> <p>Use knowledge of addition and subtraction of</p>	Model	Calculations		$\frac{1}{5}$ of 30 = 6 $30 \div 5 = 6$ $6 \times 3 = 18$ $\frac{3}{5}$ of 30 = 18	First	Then	Now				$\frac{5}{7}$	$\frac{5}{7} - \frac{2}{7}$	$\frac{3}{7}$	<p>Move from the bar model to the number line and then the abstract, continuing to show the pictorial to support.</p>   <table border="1" data-bbox="1155 1015 1413 1075"> <thead> <tr> <th colspan="10">1</th> </tr> </thead> <tbody> <tr> <td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td> </tr> </tbody> </table> $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$ <table border="1" data-bbox="1155 1161 1413 1222"> <thead> <tr> <th colspan="10">1</th> </tr> </thead> <tbody> <tr> <td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td> </tr> </tbody> </table> <table border="1" data-bbox="1155 1246 1413 1307"> <thead> <tr> <th colspan="10">1</th> </tr> </thead> <tbody> <tr> <td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td><td>$\frac{1}{10}$</td> </tr> </tbody> </table>	1										$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	1										$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	1										$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	<p>_____ is equivalent to _____.</p> <p>_____ and _____ are related fractions because the denominator, "_____", is a multiple of the other denominator "_____".</p> <p>What has stayed the same?</p> <p>What has changed?</p>	
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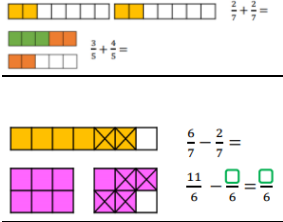
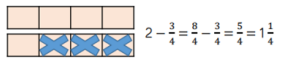
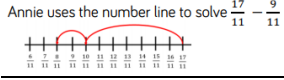
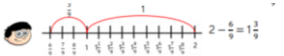


Arden Primary School Calculation Policy

		<p>fractions to find different ways to partition - use the part, part, whole model.</p> <p>.</p>  <p>Explore addition and subtraction through the use of the fraction wall.</p> 	$\frac{8}{9} - \frac{3}{9} = \frac{5}{9}$		
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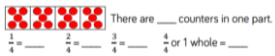




Arden Primary School Calculation Policy

<p>Year 4</p> <p>Add two or more fractions with the same denominator.</p> <p>Subtract two fractions with the same denominator.</p> <p>Subtract from whole amounts.</p>	<p>As Year 3, including examples where the fraction is improper and where more than two fractions are used in the calculation.</p> <p>Understand that whole numbers have equivalent numerators and denominators. Explore this using paper strips.</p> 	<p>As Year 3, including examples where the fraction is improper and where more than two fractions are used in the calculation.</p>  <p>Use bar models to illustrate the subtraction calculation, showing larger whole numbers as more than one strip.</p> 	<p>As Year 3, including examples where the fraction is improper and where more than two fractions are used in the calculation.</p>  <p>Annie uses the number line to solve $\frac{17}{11} - \frac{9}{11}$</p> <p>Show number lines alongside the bar model to illustrate the subtraction calculation and move to the abstract.</p>  $2 - \frac{6}{9} = \frac{18}{9} - \frac{6}{9} = \frac{12}{9} = 1\frac{3}{9}$		
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Arden Primary School Calculation Policy

<p>Calculate fractions of a quantity.</p>	<p>As Year 3 plus...</p> <p>Use counters and place value counters to find unit and non unit fractions of amounts. Understand the 'divide by the denominator, multiply by the numerator' rule and apply when using counters.</p>  	<p>As Year 3 plus...</p> <p>Represent the calculation using a bar model.</p>  <p>$\frac{5}{9}$ of 369 = 205</p>	<p>Moving to...</p> $2 - \frac{6}{9} = 1\frac{3}{9}$ <p>As Year 3 plus...</p> <p>Show all steps in the calculation using the 'divide by the denominator, multiply by the numerator' rule with increasing complexity. Use all multiplication facts from Year 4 and relate to division.</p> <p>Find $\frac{5}{9}$ of 369. $369 \div 9 = 41$ $41 \times 5 = 205$</p>		
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Arden Primary School Calculation Policy

Year 5

Add and subtract fractions with the same denominator and denominators that are multiples of the same number.

Add and subtract fractions within one.

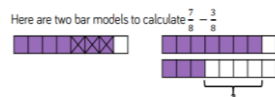
Add three or more fractions.

As Year 4 for fractions with the same denominator.

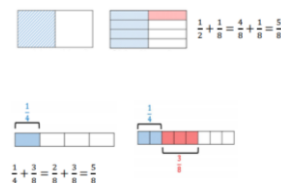
Use paper strips and circles to identify equivalent fractions when working with fractions whose denominators are multiples of the same number.



As Year 4 for fractions with the same denominator.



Represent the paper strips using bar models that show the equivalent fractions.



Add three or more fractions including greater complexity using bar models alongside calculations.



Show subtraction using crosses on a bar model.

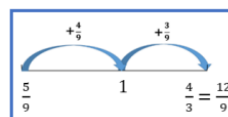


As Year 4 for fractions with the same denominator.

Represent the calculation in its abstract form alongside the bar model, beginning to recognise the arithmetical connections between numerators and denominators.

$$\frac{2}{6} + \frac{3}{12} + \frac{1}{3} = \frac{4}{12} + \frac{3}{12} + \frac{4}{12} = \frac{11}{12}$$

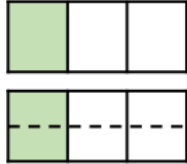

Find the difference using a number line.



Some content taken/adapted from:
DfE National Curriculum
NCETM
White Rose Maths



Arden Primary School Calculation Policy

<p>Divide fractions by integers.</p> <p>Find fractions of an amount.</p>	<p>Dexter is calculating $\frac{1}{2} \times \frac{1}{3}$ by folding paper. He folds a piece of paper in half. He then folds the half into thirds. He shades the fraction of paper he has created. When he opens it up he finds he has shaded $\frac{1}{6}$ of the whole piece of paper.</p> <p>$\frac{1}{3} \times \frac{1}{2}$ means $\frac{1}{3}$ of a half. Folding half the paper into three equal parts showed me that $\frac{1}{3} \times \frac{1}{2} = \frac{1}{6}$.</p> <p>Represent the division of fractions by integers using paper strips.</p> <p>As Year 5.</p>	<p>$\frac{4}{5} \times \frac{3}{4}$</p> <p>Notice that across the top, we have shaded in 4 out of 5 across the top to represent the four-fifths. Then we shaded 3 out of 4 vertically to show three-fourths.</p> <p>Now we can use the diagram to get the product.</p> <p>The total number of spaces is the denominator and the shaded number of spaces is the numerator. This diagram shows the fraction $\frac{12}{20}$.</p> <p>Show how to divide fractions by integers using bar models.</p>  <p>$\frac{1}{3} \div 2 = \frac{1}{6}$</p> <p>$\frac{1}{3} \div 2 = \frac{1}{6}$</p>  <p>As Year 5.</p>	<p>$\frac{2}{3} \times \frac{5}{7} = \frac{10}{21}$</p> <p>Understand that to divide fractions by integers, you need only divide the numerator.</p> <p>$\frac{4}{9} \div 2 = \frac{4 \div 2}{9} = \frac{2}{9}$</p> <p>As Year 5.</p>		
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